

## Week 6: Binomial and Poisson Models

### Exercise 1: Pirate Eagles

The pirate eagle data (`library(MASS);data(eagles)`)—Knight, R. L. and Skagen, S. K. 1988. Agonistic asymmetries and the foraging ecology of Bald Eagles. *Ecology* 69, 1188–1194) contains counts of successful salmon pirating attempts by one bald eagle on another. The columns are described in the help: `?eagles`.

I want you to study the relationship between the three prediction variables and the outcome, number of successful attempts.

(a) Build a series of binomial regression models—including P, A, and V as main and/or interaction effects—to predict the y values. Be sure to also fit an intercept-only model. Fit these models with `mle2()` and compare them using AIC (not  $AIC_c$ , as these are not gaussian models). You will need to manually convert the text prediction variables to 0/1 dummy variables.

(b) Interpret the model estimates. If you used a logit transform inside your binomial models, then you will need to convert them back to probability scale. The conventional way to do this is to use the same  $\exp(\beta)$  conversion that works for log-normal regression (which you did last week). Specifically, if we model the probability of a success as:

$$\Pr(y_i = 1|\alpha, \beta) = \frac{\exp(\alpha + \beta x_i)}{1 + \exp(\alpha + \beta x_i)},$$

then the proportional change in the odds of a success is given by  $\exp(\beta)$ . The proof is as simple as you might expect. Let  $p = \Pr(y_i = 1|\alpha, \beta)$ . The odds of success are defined as  $p/(1 - p)$ . So the proportional change in odds induced by a unit change in  $x_i$  is just the odds when  $x_i = x + 1$  divided by the odds when  $x_i = x$ . Simplification yields the answer, which is just  $\exp(\beta)$ . As before, if  $\exp(\beta) = 2$ , then a unit increase in  $x_i$  doubles the odds. If  $\exp(\beta) = 0.5$ , then a unit increase in  $x_i$  halves the odds.

If you use the alternative form of the logit:

$$\Pr(y_i = 1|\alpha, \beta) = \frac{1}{1 + \exp(\alpha + \beta x_i)},$$

then the proportional change in odds is given by  $\exp(-\beta)$ —it just flips the sign on the coefficients.

(c) Represent the model predictions graphically. There are lots of ways to do this. Be creative.

### Exercise 2: Elephants in love

The data in the file `elephants.csv` are the numbers of successful matings—in a single season—by individual male African elephants, of different ages (J.H. Poole. 1989. Mate guarding, reproductive success and female choice in African elephants. *Animal Behaviour* 37:842–849). Male elephants can reproduce by about 15 years of age, but most males this young aren't very successful. This is because males compete vigorously for matings, and older males tend to win these competitions. Some people think that the reason elephants have such long lives is that selection favors long lived males, because older males get most of the matings. If the mating system or the nature of competition were different, selection might not favor males' living so long. (I suppose one must

ignore the female half of the species, which lives even longer than the male half, to take this theory seriously.)

I want you to use a Poisson regression to study the relationship between age and mating success.

- (a) Plot number of matings (vertical axis) against age (horizontal axis).
- (b) Fit a Poisson model—matings  $\sim$  age—using `mle2()`. Compare this model to the intercept-only model. Interpret the results, including the confidence intervals.
- (c) Plot the data again, and now overlay the predicted trend, using your estimated parameters.

### Exercise 3: Las salamandras del norte

The data in `salamanders.csv` are abundances of salamanders (*Plethodon elongatus*) from 47 plots in northern California (H.H. Welsh and A.J. Lind, 1995. *Journal of Herpetology* 29:198–210). You also are given the percent forest cover and forest age for each sampled site.

- (a) Plot the abundance against percent forest cover. Is the effect of cover approximately linear?
- (b) Model abundance as a linear function of percent cover, and compare this model to an alternative simpler model. Use a Poisson distribution for abundance in each case. Plotting your fit over the data, are you satisfied with this model or not?
- (c) Try adding another model to your comparison set:  $\lambda = \alpha \exp(\beta x_i)$ . Compare this model to the other models you have fit, and also plot it over the data.
- (d) Finally, can you think of a biological reason that salamanders might have been under-sampled in the more open sites? That is, imagine salamanders are actually more abundant in the open sites than the data suggest. What might explain the mis-match between the data collected and the reality?